

$$\vec{V}_{D \in \mathcal{E} / R_0} = a_1 \dot{\beta} \vec{z}_1 - r_5 (\dot{\beta} + \dot{\theta}) \vec{z}_1 \quad (\text{image 1})$$

I. 2 Roulement sans glissement aux points D et E

• en E

$$\vec{V}_{E \in \mathcal{E} / R_0} = \vec{V}_{E \in \mathcal{B} / R_0}$$

$$r_2 \dot{\theta} = r_3 \dot{\varphi} \Rightarrow$$

$$\dot{\varphi} = \frac{r_2}{r_3} \dot{\theta} = \frac{r_2}{r_3} \omega$$

• En D

$$\vec{V}_{D \in \mathcal{E} / R_0} = \vec{0}$$

$$a_1 \dot{\beta} - r_5 (\dot{\beta} + \dot{\theta}) = 0$$

$$(a_1 - r_5) \dot{\beta} = r_5 \dot{\theta}$$

$$\dot{\beta} = \frac{r_5}{a_1 - r_5} \dot{\theta} = \frac{r_5}{a_1 - r_5} \omega$$

3 vitesse de G.

$$\vec{V}_{G/R_0} = \vec{V}_{K/R_0} + \vec{\omega}_{\mathcal{B}/R_0} \wedge \vec{KG}$$

$$\vec{V}_{K/R_0} = b_2 \dot{\beta} \vec{z}_1, \quad \vec{\omega}_{\mathcal{B}/R_0} = \dot{\varphi} \vec{y}_1 + \dot{\beta} \vec{x}_0$$

$$\vec{KG} = z \vec{x}_3 + y \vec{y}_1$$

$$\vec{z}_1 \rightarrow \dots \rightarrow \vec{z}_3 \rightarrow \dots \rightarrow \vec{z}_1$$

$$\vec{V}_{G/R_0} = b_2 \dot{\beta} \vec{z}_1 - x \dot{\varphi} \vec{z}_3 + x \dot{\beta} \sin \varphi \vec{y}_1 + y \dot{\beta} \vec{z}_1$$

$$\vec{V}_{G/R_0} = (b_2 + y) \dot{\beta} \vec{z}_1 - x \dot{\varphi} \vec{z}_3 + x \dot{\beta} \sin \varphi \vec{y}_1$$

$$\vec{z}_3 = \cos \varphi \vec{z}_1 + \sin \varphi \vec{x}_0$$

$$\vec{V}_{G/R_0} = -x \dot{\varphi} \sin \varphi \vec{x}_0 + x \dot{\beta} \sin \varphi \vec{y}_1 + ((b_2 + y) \dot{\beta} - x \dot{\varphi} \cos \varphi) \vec{z}_1$$

$$V_x = -x \dot{\varphi} \sin \varphi, \quad V_y = x \dot{\beta} \sin \varphi$$

$$V_z = (b_2 + y) \dot{\beta} - x \dot{\varphi} \cos \varphi$$

i. Accélération de G.

$$\vec{a}_{G/R_0} = \frac{d\vec{V}_{G/R_0}}{dt} \Big|_{R_0}$$

$$\vec{a}_{G/R_0} = \dot{V}_x \vec{x}_0 + \dot{V}_y \vec{y}_1 + \dot{V}_z \vec{z}_1 + \beta \dot{V}_y \vec{z}_1 + \dot{V}_z \dot{\beta} \vec{y}_1$$

$$\text{avec } \dot{V}_x = -x \dot{\varphi}^2 \cos \varphi, \quad \dot{V}_y = x \dot{\beta} \dot{\varphi} \cos \varphi,$$

$$\dot{V}_z = x \dot{\varphi}^2 \sin \varphi$$

$$4 \cdot m_4 \cdot \omega_{R_0} \cdot \vec{V}_{G/R_0} = 2 \cdot x \dot{\beta} \dot{\varphi}^2 - (\dot{\beta}^2 (b_2 + y))$$

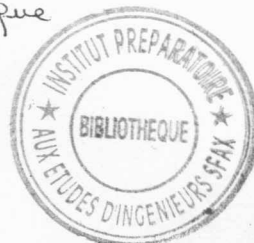
$$Z_{14} = m_4 \cdot g \cos \beta \approx 0$$

$$\Gamma_x = -x \dot{\varphi}^2 \cos \varphi$$

$$\Gamma_y = x \dot{\beta} \dot{\varphi} \cos \varphi - \dot{\beta}^2 (b_2 + y) \dot{\beta} - x \dot{\varphi} \cos \varphi$$

$$\Gamma_z = x \dot{\varphi}^2 \sin \varphi + z \dot{\beta}^2 \sin \varphi$$

Partie A. III. Dynamique



$$\varphi = 0, \quad \dot{\varphi} \neq 0$$

$$\vec{z}_3 = \vec{z}_1, \quad \vec{y}_3 = \vec{y}_1, \quad \vec{x}_3 = \vec{x}_1$$

III.1 Action sur (4)

$$\text{Roids appliqué en G. } \vec{P} = -(\underbrace{M_1 + M_2 + m_4}_{m_4}) g \vec{z}_0$$

$$\vec{H}_G(\vec{P}) = \vec{0}, \quad \vec{P} = -m_4 g (\cos \beta \vec{z}_1 + \sin \beta \vec{y}_1)$$

$$\begin{aligned} \vec{H}_K(\vec{P}) &= (x \vec{x}_0 + y \vec{y}_1) \wedge (m_4 g \vec{z}_0) \\ &= -m_4 g \begin{pmatrix} x \\ y \\ 0 \end{pmatrix} \wedge \begin{pmatrix} 0 \\ \sin \beta \\ \cos \beta \end{pmatrix} \quad \vec{g} = -g \vec{z}_0 \\ &= -m_4 g \begin{pmatrix} y \cos \beta \\ x \cos \beta \\ x \sin \beta \end{pmatrix} \end{aligned}$$

$$\left\{ \mathcal{E}_{(P)} \right\}_K = \left\{ \begin{array}{c|c} 0 & -m_4 g y \cos \beta \\ -m_4 g \sin \beta & m_4 g x \cos \beta \\ -m_4 g \cos \beta & -m_4 g x \sin \beta \end{array} \right\}_{(\vec{x}_0, \vec{y}_1, \vec{z}_1)}$$

• Action de 3 sur (4) en K

$$\left\{ \mathcal{E}_{4/3} \right\}_K = \left\{ \begin{array}{c|c} x_{34} & L_{14} \\ y_{34} & 0 \\ z_{14} & N_{14} \end{array} \right\}_{(x_0, y_1, z_1)}$$

• action de (3) sur (4) en K.

$$\left\{ \mathcal{E}_{4/3} \right\}_K = \left\{ \begin{array}{c|c} 0 & 0 \\ N_J & G_J \\ 0 & 0 \end{array} \right\}_{(\vec{x}_0, \vec{y}_1, \vec{z}_1)}$$

III.3 Théorème de la résultante dynamique

$$\begin{cases} X_{14} = -m_4 x \dot{\varphi}^2 \\ N_J + Y_{14} - m_4 g \sin \beta = (2x \dot{\beta} \dot{\varphi} - \dot{\beta}^2 (b_2 + y)) m_4 \\ Y_{14} = m_4 g \sin \beta + m_4 (2x \dot{\beta} \dot{\varphi} - \dot{\beta}^2 (b_2 + y)) - \frac{3m_4 g x \cos \beta}{2\beta} \end{cases}$$

Partie A: Géométrie des masses

(I)

I.1. Position du centre G de l'ensemble (4)

- cylindre (masse M)

$$\vec{KG}_c = \frac{H}{2} \vec{x}_3 + (L - a_4) \vec{y}_1$$

- tige (masse m_t)

$$\vec{KG}_t = (\frac{L}{2} - a_4) \vec{y}_1$$

- disque (masse m)

$$\vec{KG}_d = -a_4 \vec{y}_1$$

On applique la relation du barycentre

$$\vec{KG} = \frac{M \vec{KG}_c + m_t \vec{KG}_t + m \vec{KG}_d}{M + m_t + m}$$

$$x = \frac{M \frac{H}{2}}{M + m_t + m}$$

$$y = \frac{ML + m_t(\frac{L}{2} - a_4) - ma_4}{M + m_t + m}$$

I.2. Matrices centrales d'inertie

- cylindre:

$$[I_{ccy}] = \begin{bmatrix} \frac{Mr^2}{2} & 0 & 0 \\ 0 & \frac{Mr^2}{4} + \frac{MH^2}{12} & 0 \\ 0 & 0 & \frac{Mr^2}{4} + \frac{MH^2}{12} \end{bmatrix} (\vec{x}_3, \vec{y}_1, \vec{z}_3)$$

- tige:

$$[I_{ttg}] = \begin{bmatrix} \frac{m_t L^2}{12} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \frac{m_t L^2}{12} \end{bmatrix} (\vec{x}_3, \vec{y}_1, \vec{z}_3)$$

- disque:

$$[I_{disque}] = \begin{bmatrix} \frac{mr^2}{4} & 0 & 0 \\ 0 & \frac{mr^2}{2} & 0 \\ 0 & 0 & \frac{mr^2}{4} \end{bmatrix} (\vec{x}_3, \vec{y}_1, \vec{z}_3)$$

I.3. Matrice d'inertie de l'ensemble (4).

le plan $(K, \vec{x}_3, \vec{y}_1)$ est un plan de symétrie, par suite (K, \vec{z}_3) est un axe principal d'inertie

$$[I_K] = \begin{bmatrix} A_u & -F_u & 0 \\ -F_u & B_u & 0 \\ 0 & 0 & C_u \end{bmatrix} (\vec{x}_3, \vec{y}_1, \vec{z}_3)$$

$$v_3 = x_4 \sin \varphi = 0$$

$$A_u = \frac{Mr^2}{2} + HL^2 + \frac{m_t L^2}{12} + m_t (\frac{L}{2} - a_4)^2 + \frac{mr^2}{4} + ma_4^2$$

$$B_u = \frac{Mr^2}{4} + \frac{MH^2}{12} + \frac{m_t r^2}{2} + \frac{MH^2}{4}$$

$$C_u = \frac{Mr^2}{4} + \frac{MH^2}{12} + \frac{MH^2}{4} + HL^2 + \frac{m_t L^2}{12} + (\frac{L}{2} - a_4)^2 m_t + \frac{mr^2}{4} + ma_4^2$$

$$F_u = \frac{MH}{2} L$$

Partie A.II. Cinématique.

II.1 Vitesses

$$\vec{V}_{N/R_0} = \vec{V}_{O/R_0} + \vec{\omega}_{1/R_0} \wedge \vec{OA}$$

$$\vec{V}_{O/R_0} = \vec{0}, \quad \vec{\omega}_{1/R_0} = \dot{\beta} \vec{x}_3, \quad \vec{OA} = a_1 \vec{y}_1$$

$$\vec{V}_{N/R_0} = a_1 \dot{\beta} \vec{z}_1$$

$$\vec{V}_{I/R_0} = \vec{V}_{O/R_0} + \vec{\omega}_{1/R_0} \wedge \vec{OI}$$

$$\vec{OI} = a_2 \vec{x}_3 + b_2 \vec{y}_1$$

$$\vec{V}_{I/R_0} = b_2 \dot{\beta} \vec{z}_1$$

$$\vec{V}_{K/R_0} = \vec{V}_{O/R_0} + \vec{\omega}_{1/R_0} \wedge \vec{OK}$$

$$\vec{OK} = a_3 \vec{x}_3 + b_3 \vec{y}_1$$

$$\vec{V}_{K/R_0} = b_3 \dot{\beta} \vec{z}_1$$

$$\vec{V}_{EE2/R_1} = \vec{V}_{K/R_1} + \vec{\omega}_{2/R_1} \wedge \vec{AE}$$

$$\vec{V}_{K/R_1} = \vec{0}, \quad \vec{\omega}_{2/R_1} = \dot{\theta} \vec{x}_3, \quad \vec{AE} = c_1 \vec{x}_3 + c_2 \vec{y}_1$$

$$\vec{V}_{EE2/R_1} = c_2 \dot{\theta} \vec{z}_1$$

$$\vec{V}_{EE3/R_1} = \vec{V}_{I/R_1} + \vec{\omega}_{3/R_1} \wedge \vec{IE}$$

$$\vec{V}_{I/R_1} = \vec{0}, \quad \vec{\omega}_{3/R_1} = \dot{\psi} \vec{y}_1, \quad \vec{IE} = -r_3 \vec{x}_3 - c_3 \vec{y}_1$$

$$\vec{V}_{EE3/R_1} = r_3 \dot{\psi} \vec{z}_1$$

$$\vec{V}_{DE5/R_2} = \vec{V}_{A/R_2} + \vec{\omega}_{4/R_2} \wedge \vec{AD}$$

$$\vec{V}_{A/R_2} = m_4 g \sin \beta = R \sin \beta \varphi - \beta (b_4 + y) / m_4$$

$$r_{14} = m_4 g \sin \beta + m_4 (\dot{\alpha} \beta \dot{\varphi} - \beta (b_4 + y)) - \frac{3m_4 g x_{14}}{2R}$$

III.3) Moment dynamique en K.

$$\vec{\sigma}_K(4/R_0) = m_4 \vec{KG} \wedge \vec{V}_{K/R_0} + \left[\vec{I}_K(u) \right] \vec{\omega}_{4/R_0}$$

$$\vec{\sigma}_K(4/R_0) = \frac{d\vec{\sigma}_K(4/R_0)}{dt} + m_4 \vec{V}_{K/R_0} \wedge \vec{V}_{G/R_0}$$

$$\begin{aligned} \vec{KG} \wedge \vec{V}_{K/R_0} &= (x \vec{x}_3 + y \vec{y}_1) \wedge (b_2 \dot{\beta} \vec{z}_1) \\ &= -b_2 \dot{\beta} x \cos \varphi \vec{y}_1 + b_2 \dot{\beta} y \vec{x}_0 \end{aligned}$$

$$\begin{aligned} \vec{\omega}_{4/R_0} &= \dot{\varphi} \vec{y}_1 + \dot{\theta} (\cos \varphi \vec{x}_3 + \sin \varphi \vec{z}_3) \\ \left[\vec{I}_K(u) \right] \cdot \vec{\omega}_{4/R_0} &= \begin{bmatrix} A_4 & -F_4 & 0 \\ -F_4 & B_4 & 0 \\ 0 & 0 & C_4 \end{bmatrix} \begin{bmatrix} \dot{\theta} \cos \varphi \\ \dot{\varphi} \\ \dot{\theta} \sin \varphi \end{bmatrix} \end{aligned}$$

$$= \begin{bmatrix} A_4 \dot{\theta} \cos \varphi - F_4 \dot{\varphi} \\ -F_4 \dot{\theta} \cos \varphi + B_4 \dot{\varphi} \\ C_4 \dot{\theta} \sin \varphi \end{bmatrix}$$

$$(A_4 \dot{\theta} \cos \varphi - F_4 \dot{\varphi}) \vec{x}_3 +$$

$$(-F_4 \dot{\theta} \cos \varphi + B_4 \dot{\varphi}) \vec{y}_1 +$$

$$C_4 \dot{\theta} \sin \varphi \vec{z}_3$$

$$\frac{d\vec{\sigma}_K}{dt} \Big|_{R_0} = (m_4 b_2 \dot{\beta} \dot{\varphi} \cos \varphi) \vec{y}_1 +$$

$$\dot{\theta} (B_4 \dot{\varphi} - F_4 \dot{\theta} \cos \varphi - m_4 b_2 \dot{\beta} x \cos \varphi) \vec{z}_1$$

$$- A_4 \dot{\theta} \dot{\varphi} \sin \varphi \vec{x}_3 + (A_4 \dot{\theta} \cos \varphi - F_4 \dot{\varphi}) (\dot{\theta} \sin \varphi \vec{x}_1 - \dot{\varphi} \vec{z}_3)$$

$$+ C_4 \dot{\theta} \dot{\varphi} \cos \varphi \vec{z}_3 + C_4 \dot{\theta} \sin \varphi (\dot{\varphi} \vec{x}_3 - \dot{\theta} \cos \varphi \vec{y}_1)$$

$$\frac{d\vec{\sigma}_K}{dt} \Big|_{R_0} = \dot{\beta} (B_4 \dot{\varphi} - F_4 \dot{\theta} - m_4 b_2 \dot{\beta} x) \vec{z}_1 +$$

$$- (A_4 \dot{\theta} - F_4 \dot{\varphi}) \dot{\varphi} \vec{z}_1 + C_4 \dot{\theta} \dot{\varphi} \vec{z}_1$$

$$\begin{aligned} m_4 \vec{V}_{K/R_0} \wedge \vec{V}_{G/R_0} &= m_4 b_2 \dot{\beta} \vec{z}_1 \wedge (b_2 + y) \dot{\beta} - x \dot{\varphi} \vec{z}_1 \\ &= \vec{0} \end{aligned}$$

$$\vec{\sigma}_K(4/R_0) = (B_4 \dot{\beta} \dot{\varphi} - F_4 \dot{\theta} \dot{\beta} - m_4 b_2 \dot{\beta}^2 x + (C_4 - A_4) \dot{\theta} \dot{\varphi} + F_4 \dot{\varphi}^2) \vec{z}_1$$

Equations dynamiques

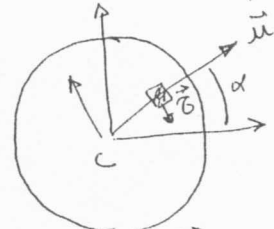
$$\begin{cases} A_4 - m_4 g y \cos \beta = 0 \\ C_4 + m_4 g x \cos \beta = 0 \\ N_{14} \mp (B_4 \dot{\beta} \dot{\varphi} + F_4 (\dot{\varphi}^2 - \dot{\theta}^2 \dot{\beta})) - m_4 b_2 \dot{\beta}^2 + (C_4 - A_4) \dot{\theta} \dot{\varphi} = 0 \end{cases}$$

III.4 Expression de N_J

On considère une surface d'appui circulaire de rayon R.

la pression étant uniforme:

$$p = \frac{N_J}{S} = \frac{N_J}{\pi R^2}$$



$$\vec{F} = -\vec{\sigma} \vec{v} = -p \cdot \vec{v}$$

$$\text{à la limite de l'ordre } \vec{F} = -\vec{\sigma} ds \vec{v} = -\vec{\sigma} r dr d\alpha \vec{v}$$

$$\begin{aligned} d\vec{M}_C &= \vec{C}H \wedge d\vec{F} \\ &= -r \vec{u} \wedge \vec{\sigma} r dr d\alpha \vec{v} \\ &= -\vec{\sigma} R^2 dr d\alpha \vec{z} \end{aligned}$$

$$\vec{M}_J = \int \vec{\sigma} R^2 dr d\alpha = \frac{2\pi \vec{\sigma} R^3}{3}$$

$$C_J = - \frac{2\pi \vec{\sigma} R^3}{3} = - \frac{2}{3} N_J R$$

$$N_J = |C_J| \frac{3}{2R}$$

III.5 inconnus de liaisons.

$$N_J = 3 \frac{m_4 g x \cos \beta}{2R}$$

$$L_{14} = m_4 g y \cos \beta$$

$$Y_{14} = m_4 g \sin \beta + m_4 (2x \dot{\beta} \dot{\varphi} - \dot{\beta}^2 (b_2 + y)) - \frac{3m_4 g x \cos \beta}{2R}$$

Partie C-II - Asservissement de position d'un arce du bras robotisé

II-1 : Simplification du schéma fonctionnel de la figure 6 :

$$\Omega_m(p) = \frac{1}{J_m p + f_m} \left[\frac{k_c}{R} (U(p) - k_e \Omega_m(p)) - \frac{1}{e} \left(C_r(p) + \frac{1}{e} (J_c p + f_c) \Omega_m(p) \right) \right]$$

\Leftrightarrow

$$\left[1 + \frac{k_e k_c / R}{J_m p + f_m} + \frac{1}{e^2} \frac{J_c p + f_c}{J_m p + f_m} \right] \Omega_m(p) = \frac{k_c / R}{J_m p + f_m} U(p) - \frac{1/e}{J_m p + f_m} C_r(p)$$

\Leftrightarrow

$$\left[\left(J_m + \frac{J_c}{e^2} \right) p + \left(f_m + \frac{f_c}{e^2} \right) + \frac{k_e k_c}{R} \right] \Omega_m(p) = \frac{k_c}{R} U(p) - \frac{1}{e} C_r(p)$$

\Rightarrow

$$\Omega_m(p) = T_1(p) U(p) - T_2(p) C_r(p)$$

avec

$$T_1(p) = \frac{K_1}{1 + \tau_{em} p} \quad \text{et} \quad T_2(p) = \frac{K_2}{1 + \tau_{em} p}$$

$$\tau_{em} = \frac{R J_e}{k_e k_c + f_e R} : \text{Constante de temps électromécanique}$$

$$K_1 = \frac{k_c}{k_e k_c + R f_e} : \text{Gain statique de } T_1(p)$$

$$K_2 = \frac{R}{e (k_e k_c + R f_e)} : \text{Gain statique de } T_2(p)$$

$$J_e = J_m + \frac{J_c}{e^2} : \text{Inertie équivalente ramenée sur l'arbre du moteur.}$$

$$f_e = f_m + \frac{f_c}{e^2} : \text{Coef. de frottement visqueux équivalent ramenée sur l'arbre du moteur.}$$

II-2: A partir de la réponse indicielle de $T_1(p)$ à un échelon de tension d'amplitude 25V:

On a:

$$\omega_m(\infty) = 25 K_1 = 200 \text{ rad.s}^{-1} \Rightarrow K_1 = 8 \text{ rad.s}^{-1} \text{ V}^{-1}$$

à 63% de $\omega_m(\infty)$ on trouve $\tau_{em} = 10 \text{ ms}$ *

II-3: schéma fonctionnel de la figure 8.

a) Fonction de transfert en boucle fermée:

$$\Theta_c(p) = H_1(p) \Theta_{ref}(p) - H_2(p) C_r(p)$$

$$\text{avec } H_1(p) = \left. \frac{\Theta_c(p)}{\Theta_{ref}(p)} \right|_{C_r=0} = \frac{\frac{\alpha A K_1}{e \tau_{em}}}{p^2 + \frac{1}{\tau_{em}} p + \frac{\alpha A K_1}{e \tau_{em}}}$$

$$H_2(p) = \left. \frac{\Theta_c(p)}{C_r(p)} \right|_{\Theta_{ref}=0} = \frac{\frac{K_2}{e \tau_{em}}}{p^2 + \frac{1}{\tau_{em}} p + \frac{\alpha A K_1}{e \tau_{em}}} *$$

Equation caractéristique:

$$p^2 + \frac{1}{\tau_{em}} p + \frac{\alpha A K_1}{e \tau_{em}} = p^2 + 2 m \omega_0 p + \omega_0^2$$

Par identification, on déduit:

$$\omega_0 = \sqrt{\frac{\alpha A K_1}{e \tau_{em}}} : \text{ pulsation propre non amortie (rad/s)}$$

$$m = \frac{1}{2} \sqrt{\frac{e}{\alpha A K_1 \tau_{em}}} : \text{ coefficient d'amortissement.}$$

b: Calcul de A pour avoir $m=0,7$.

$$\alpha = 0,8 \text{ V/rad} ; K_1 = 8 \text{ rad.s}^{-1} \text{ V}^{-1} ; \tau_{em} = 10 \text{ ms et } \rho = 5$$

$$A = \frac{\rho}{4m^2 \alpha K_1 \tau_{em}}$$

$$\text{A.N: } A = \frac{50}{4 \cdot (0,7)^2 \cdot 0,8 \cdot 8 \cdot 0,01} = 398,6$$

$$\omega_0 = \sqrt{\frac{0,8 \cdot 398,6 \cdot 8}{50 \cdot 0,01}} = 71,43 \text{ rad/s}$$

$$\text{Déphasement: } D\% = 100 \cdot e^{-\frac{m\pi}{\sqrt{1-m^2}}}$$

$$\text{A.N: } \boxed{D\% = 4,6\%}$$

$$\text{Temps de pic: } T_p = \frac{\pi}{\omega_0 \sqrt{1-m^2}}$$

$$\text{A.N: } \boxed{T_p = 0,062 \text{ s}}$$

c- Etude de la précision statique

$$\boxed{\mathcal{E}_1(p) = \Theta_{ref}(p) - \Theta_c(p) = [1 - H_1(p)] \Theta_{ref}(p) + H_2(p) C_r(p)}$$

$$\text{avec } H_1(p) = \frac{\omega_0^2}{p^2 + 2m\omega_0 p + \omega_0^2}$$

$$H_2(p) = \frac{K_2}{\alpha A K_1} \cdot \frac{\omega_0^2}{p^2 + 2m\omega_0 p + \omega_0^2} = \frac{K_2}{\alpha A K_1} H_1(p)$$

$$\boxed{\mathcal{E}_1(p) = \frac{p(p + 2m\omega_0)}{p^2 + 2m\omega_0 p + \omega_0^2} \Theta_{ref}(p) + \frac{K_2}{\alpha A K_1} \frac{\omega_0^2}{p^2 + 2m\omega_0 p + \omega_0^2} C_r(p)}$$

$$\Theta_{ref}(t) = t \cdot u(t) \xrightarrow{T.L.} \Theta_{ref}(p) = \frac{1}{p^2}$$

$$C_r(t) = 100 \cdot u(t) \xrightarrow{T.L.} C_r(p) = \frac{100}{p}$$

Théorème de la valeur finale

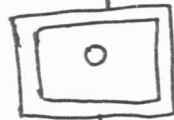
$$E_1(\infty) = \lim_{p \rightarrow 0} p E_1(p)$$

soit

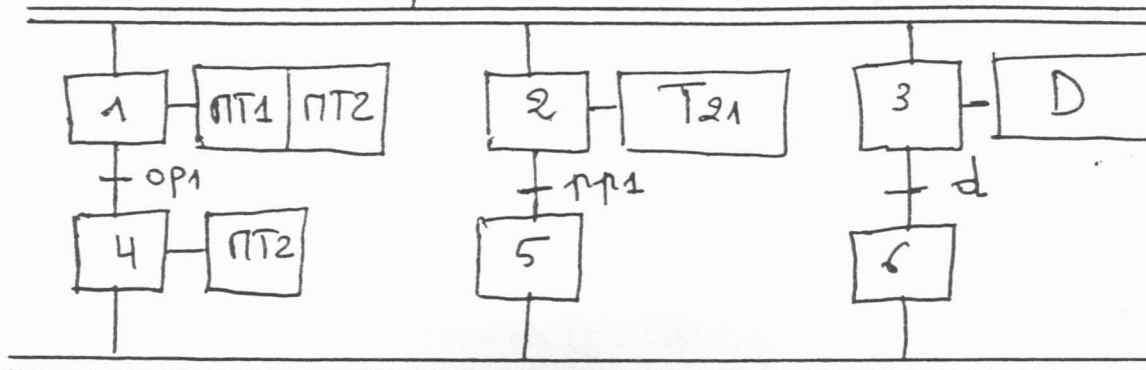
$$E_1(\infty) = \frac{2m}{\omega_0} + \frac{100 K_2}{\alpha A K_1}$$

A.N: $E_1(\infty) = 0,0196 + 0,026 = 0,049$

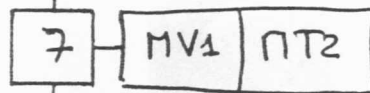
$$E_1(\infty) = 0,049 \text{ soit } 4,9\%$$



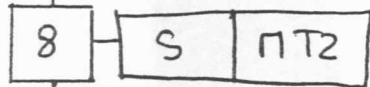
$$+ Dcy \cdot \pi p_2 \cdot v_{1b} \cdot v_{2h} \cdot v_{3r} \cdot \overline{op_2}$$



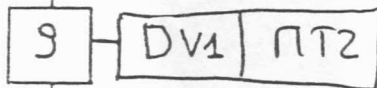
$= 1$



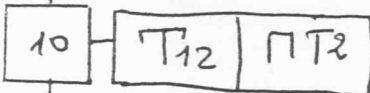
$+ v_{1h}$



$+ \Delta \cdot op_2$



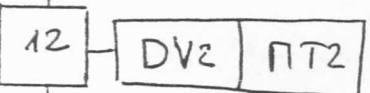
$+ v_{1b}$



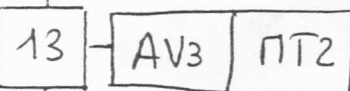
$+ \pi p_1$



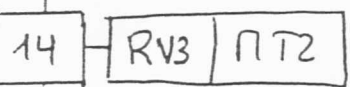
$+ d$



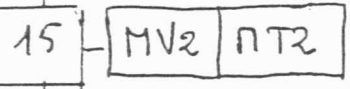
$+ v_{2b}$



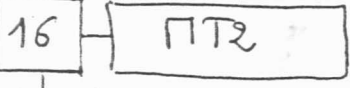
$+ v_{3a}$



$+ v_{3r}$



$+ v_{2h}$



$+ 40\Delta / X_{16}$

C.I.2)

Graphet G₁ modifié

